

## FROM TIMED AUTOMATA TO DEVS MODELS

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### ABSTRACT

In this paper, we present the formal transformation of Timed Input/Output Automata into simulation models, expressed in the DEVS formalism. This transformation takes place in an approach of a validation of high-level specifications by simulation. The validation is based on the simulation of a coupled model built with the system to be controlled and the control specifications. An example of this approach is given in the paper.

### 1 INTRODUCTION

Many formalisms have been developed to support verification and validation of formal specifications of control systems (Gajski, Vahid, Narayan, and Gong 1994; Peterson 1981; Alur and Dill 1994; Bolognesi, Lucidi and Trigila 1994).

Timed automata and variants have been used for these kinds of purposes (Alur and Kurshan 1996; Bengtsson, Larsen, Larsson, Pettersson and Wang 1996; Daws, Olivero, Tripakis and Yovine 1996; Henzinger and Ho 1995). Some works are based on the use of simulation technics of timed automata with the objective of establishing a correspondence between the states of a model M1 regarded as an implementation and a specification model M2.

We propose another approach in which we consider that the high level specification of a control system, expressed by a timed automaton, will be verified by simulation of a coupled model built with this specification and the model of the system to be controlled. The simulation models are represented in the framework of the DEVS formalism (Zeigler 1976; Zeigler 1989; Zeigler, Praehofer and Kim 2000; Giambiasi, Escude and Ghosh 2000).

The DEVS formalism has a clean operational semantics and a clean interpretation of the model elements in the real world. DEVS define a method of abstraction of dynamic

systems that allows building timed simulation models (deterministic models) with a good accuracy. In other words, DEVS is well adapted to represent timed behavior of real systems. But DEVS does not adapt well to high level specifications of discrete event control systems. This due to the fact that at the first levels of specifications, the model can be undeterministic and the occurrence times of events are not defined precisely. While, Timed Automata are well adapted for these high levels of specification, it is not well adapted to represent a precise timed behavior deduced from the analysis of a real system with explicit state variables.

Consequently, we propose a methodology (Figure 1) based on the use of these two paradigms:

- Timed Automata for the high level specification of the control part,
- DEVS to represent the behavior of the system to be controlled.

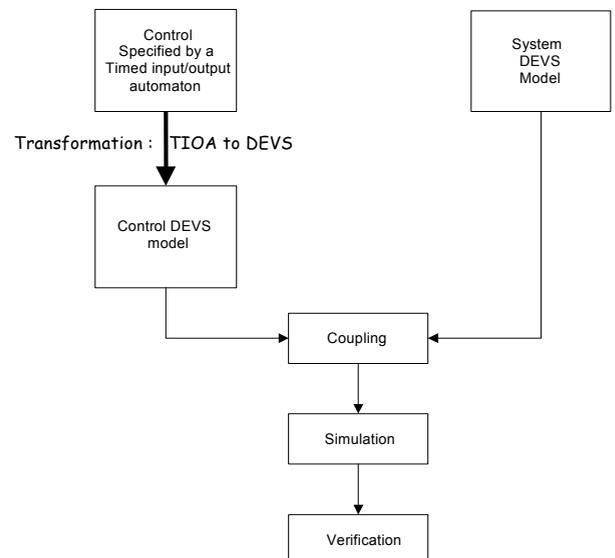


Figure 1: Our Methodology

In order to verify the specification with an accurate timing, we propose to transform T.A. into a DEVS model and to verify it by simulating the coupled model (control part coupled with the model of the controlled system).

Then, in a first step, we have to define a formal transformation of a Timed Automaton into a DEVS model.

In this paper, first we give a brief recall on timed automata and on DEVS formalism. Next, we present the method for the formal transformation of a timed automata into a DEVS model. Finally, we illustrate our approach by a complete example.

## 2 RECALL

### 2.1 Timed Automata (Springinveld, Vaandrager and D'Argenio 2001)

Timed Input/Output Automata are a particular class of timed automata (Alur and Dill 1994) with “good” properties, such as deterministic behavior, separation between input and output activity and input enabling.

A Bounded Timed Automata Model, a variant of Alur and Dill's model (Alur and Dill 1994) proposed by Lynch and Al (Gawlick, Segala, S\_gaard-Andersen and Lynch 1994) is a finite automaton with a timing annotation. This annotation allows to express timing conditions for the state transitions, to determine values used for updating clocks, and to provide conditions, under which the model can remain in a given state. A TIOA is defined as Bounded Timed Domain Automata BTDA (Springintveld and Vaandrager 1996) together with a partitioning the set of actions into Input and Output actions (or events).

#### 2.1.1 Finite Automaton or Finite Labeled Transition System

A labeled transition system (LTS) is a rooted, edge labeled multigraph. Formally, a LTS is an algebraic structure

$$\mathbf{A} = \langle Q, E, \Sigma, \text{src}, \text{act}, \text{trg}, q^0 \rangle,$$

where:

- $Q$  is a set of states,
- $E$  is a set of transitions,
- $\Sigma$  is a set of events.
- $\text{src}: E \rightarrow Q$  which associates a source state to each transition,
- $\text{act}: E \rightarrow \Sigma$  which associates an event to each transition,
- $\text{trg}: E \rightarrow Q$  which associates a target state to each transition.

Initial conditions:

- $q^0$  is the initial state.

So we write:

$\delta: q \rightarrow^a q'$ , the transition with :

$$\text{src}(\delta) = q ; \text{act}(\delta) = a ; \text{trg}(\delta) = q'$$

**Definition 1:** An LTS  $A$  is said *lean* if each transition is fully determined by its source, event and target, as follows:

$$\text{src}(\delta) = \text{src}(\delta') \wedge \text{act}(\delta) = \text{act}(\delta') \wedge \text{trg}(\delta) = \text{trg}(\delta') \Rightarrow \delta = \delta'$$

**Definition 2:** An LTS  $A$  is said *deterministic* if it satisfies the following property:

$$\text{src}(\delta) = \text{src}(\delta') \wedge \text{act}(\delta) = \text{act}(\delta') \Rightarrow \delta = \delta'$$

**Definition 3:** An LTS  $A$  is a *finite automaton* if both  $Q$  and  $E$  are finite.

#### 2.1.2 Bounded Time Domain Automata

A bounded time domain automaton (BTDA) is an extension of finite automaton model and it is a variant of timed automaton model.

A timed automaton is typically a (finite) automaton extended with a set of clocks.

For the BTDA model, we have the following definitions :

**Definition 4:** A clock is a variable  $x$  included in a domain  $\text{dom}(x)$  of the form  $I \cup \{\infty\}$ , where  $I$  is an interval over  $\mathbb{R}$  bounded with values  $\in \mathbb{Z}$ . Let  $C$  be the set of clocks.

**Definition 5:** A term over  $C$  is an expression generated by the grammar  $z ::= x | n | z + n$ , where  $x \in C$  and  $n \in \mathbb{R}$ . Let  $T(C)$  be the set of all terms over  $C$ .

**Definition 6:** A constraint over  $C$  is a Boolean combination  $\phi$  of inequalities of the form  $z \leq z'$  or  $z < z'$  with  $z, z' \in T(C)$ . The Boolean constants are used to indicate if the constraint is realized or not. Let  $F(C)$  be the set of all these formulas.

**Definition 7:** A (simultaneous) assignment over  $C$  is a function  $A : C \rightarrow T(C)$ . Let  $M(C)$  be the set of all assignments.

**Definition 8:** A clock valuation is a vector that assigns to each clock  $x \in C$  a value in  $\text{dom}(x)$ . Let  $V(C)$  be the set of all valuations over  $C$ .

A timing annotation for a given automaton  $A$  is a tuple:

$$\mathbf{T} = \langle C, \text{Inv}, G, A, v^0 \rangle$$

where :

- $C$  is a finite set of clocks.
- $\text{Inv}: Q \rightarrow F(C)$  associates an invariant to each state. The automaton  $A$  can remain in a state as long as its invariant remains true.

- $G: E \rightarrow F(C)$  associates a guard to each transition. A transition may be taken if the guard, a clock constraint, is satisfied by the current valuation of clocks.
- $A: E \rightarrow M(C)$  associates an assignment to each transition such as :

$$\text{src}(\delta) \wedge G(\delta) \Rightarrow \bigwedge_{x \in C} (A(\delta)(x) \in \text{dom}(x)) \wedge \text{Inv}(\text{trg}(\delta))[A(\delta)]$$

holds for each  $\delta \in E$ .

Initial conditions :

- $v^0 \in V(C)$  is the initial valuation of clocks. We require  $v^0$  satisfy  $\text{Inv}(q^0)$  and  $\forall x \in C, v^0(x) \in \mathbb{Z}^\infty$ .

**Definition 9:** The addition of a clock value  $v(x)$  with a value  $d \in \mathbb{R}^{>0}$  is defined as follow :

$$\begin{aligned} (v \oplus d)(x) &= v(x) + d && \text{if } (v(x) + d) \in \text{dom}(x) \\ (v \oplus d)(x) &= \infty && \text{otherwise} \end{aligned}$$

**Definition 10:** A bounded time domain automata (BTDA) is a pair  $B = (A, T)$ , where  $A$  is a finite automaton with  $\Sigma_A \cap R = \emptyset$ , and  $T$  is a timing annotation for  $A$ .

**Definition 11:** The operational semantics  $\text{OS}(B)$  of a BTDA  $B$  is the lean LTS  $A$ , which is specified by:

- $Q_A = \{(q, v) \in Q_B \times V(C_B) \mid v \models \text{Inv}_B(q)\}$ ,
- $\Sigma_A = \Sigma_B \cup \mathbb{R}^{>0}$ ,
- $Q_A^0 = (Q_B^0, v_B^0)$ ,
- And  $\rightarrow^a$  is the smallest relation that satisfies the two following rules :

$$\forall (q, v), (q', v') \in Q_A, a \in \Sigma_B, \delta \in E_B \text{ and } d \in \mathbb{R}^{>0},$$

$$\begin{aligned} \delta: q \rightarrow^a q', v \models G_B(\delta), v' = v \circ A_B(\delta), \\ (q, v) \rightarrow^a (q', v') \\ \underline{q = q', v' = v \oplus d; \forall 0 \leq d' \leq d: v + d' \models \text{Inv}_B(q)} \\ (q, v) \xrightarrow{d} (q', v') \end{aligned}$$

We refer to the states of BTDA  $B$  as locations, to avoid confusion between the state of the BTDA and those of its operational semantics. So we have :

- discrete states  $\in Q_B \times V(C_B)$ ,
- locations  $\in Q_B$ .

### 2.1.3 Timed Input/Output Automata (Gawlick, Segala, S\_gaard-Andersen and Lynch 1994)

We recall some basic definitions on timed I/O automaton (TIOA).

In addition, some constraints will be added in order to allow the transformation of a TIOA into a discrete event simulation model. In fact, for this transformation a TIOA must be *deterministic*, with *isolated output* for excluding autonomous choice between two or more different outputs

or between performing output and accepting input. Finally, it must be *input enabling* i.e. each input is enabled only in the interior of the invariant of each location, this means that inputs are enabled as long as time can progress.

**Definition 12:** A timed input/output automaton (TIOA) is a pair  $M = (B, P)$ , where  $B$  is a BTDA and  $P = (I, O)$  is a partitioning of  $\Sigma_B$  in input events and outputs events with the following properties :

- (Determinism) If  $\text{src}(\delta) = \text{src}(\delta')$ ,  $\text{act}(\delta) = \text{act}(\delta')$  and  $G(\delta) \wedge G(\delta')$  is satisfiable then  $\delta = \delta'$ .
- (Isolated outputs) If  $\text{src}(\delta) = \text{src}(\delta')$ ,  $\text{act}(\delta) \in O$  and  $G(\delta) \wedge G(\delta')$  is satisfiable then  $\delta = \delta'$ .
- (Input enabled) each input event is enabled only in the interior of the invariant i.e. only when the invariant is verified.

The operational semantics  $\text{OS}(A)$  of a TIOA  $A$  is the same as the one of BTDA  $B$ .

## 2.2 Discrete Event Specification Formalism: DEVS

According to the literature on DEVS (Zeigler 1976; Zeigler 1989), the specification of a discrete event model is a structure,  $M$ , given by:

$$M = \langle X, S, Y, \delta_{\text{int}}, \delta_{\text{ext}}, \lambda, D \rangle$$

where  $X$  is the set of the external input events,  $S$  the set of the sequential states,  $Y$  the set of the output events,  $\delta_{\text{int}}$  is the internal transition function :

- $\delta_{\text{int}} : S \rightarrow S$  defines the state changes caused by internal events,

$\delta_{\text{ext}}$  is the external transition function :

- $\delta_{\text{ext}}: Q_M \times X_M \rightarrow S$  specifies the state changes due to external events,

$\lambda$  is the output function :

- $\lambda : S \rightarrow Y$

and the function  $D$  is the lifetime of the states:

- $D: S \rightarrow \mathbb{R}^{\geq 0} \cup \{\infty\}$ . For a given state,  $s$ ,  $D(s)$  represents the time interval during which the model will remain in the state  $s$  if no external event occurs.

A state may be viewed as passive when its lifetime is assumed to be infinite or active when the lifetime interval is assumed to be a finite real positive number, Zeigler (Zeigler 1976) introduces the concept of total states,  $TS$ , of a model as:

$$TS = \{(s, e) : s \in S, 0 < e < D(s)\}$$

where  $e$  represents the elapsed time in state  $s$ . The concept of total state is fundamental in that it permits one to specify a future state based on the elapsed time in the present state. Potential benefits may lie in its ability to implement event filtering (Ghosch and Meng-Lin 1989; Ghosch and Giambiasi 1999).

A key contribution of DEVS lies in decomposing the traditional transition function into two sub-functions: internal transition function and external transition function. The internal transition function permits one to capture the autonomous evolution of the model. The external transition function reflects the evolution of the model corresponding to externally induced input events. The output function is defined only for active states and is executed only when the elapsed time in a given state equals its lifetime. When a model is in an active state  $s_k$ , it sends an output event as defined by the output function, at the end of the lifetime of the current active state. From the simulation perspective, this implies that the output function is executed prior to the internal transition function.

### 2.3 Coupled Models

A coupled DEVS Model, DN, is a structure :

$$\mathbf{DN} = \langle X, Y, M, \text{EIC}, \text{EOC}, \text{IC} \rangle$$

Where :

- $X$  = input events set
- $Y$  = output events set
- $M$  = DEVS components set
- $\text{EIC} \subseteq \text{DN.IN} \times \text{M.IN}$  : external input coupling relation
- $\text{EOC} \subseteq \text{M.OUT} \times \text{DN.OUT}$  : external output coupling relation
- $\text{IC} \subseteq \text{M.OUT} \times \text{M.IN}$  : internal coupling relation
- $\text{DN.IN}$  and  $\text{DN.OUT}$  refer to the input and output ports of the coupled model.
- $\text{M.IN}$  and  $\text{M.OUT}$  refer to the input and output ports of component Models.

$\text{EIC}$ ,  $\text{EOC}$ ,  $\text{IC}$  specify the connections between the set of models  $M$  and input and output ports  $X, Y$ .

### 3 FROM TIOA TO ATOMIC DEVS MODEL

For this transformation, we make two hypotheses.

- i. The timestamp of a transition over an output event has a unique value (not define in a time interval).
- ii. The conditions of guards of two different transitions, with the same input event and from the same state must be expressed using different clocks. Formally:

Let  $e_1, e_2 \in E$  such that :

- $\text{src}(e_1) = \text{src}(e_2)$ ,
- $\text{act}(e_1) = \text{act}(e_2)$  and
- let  $X_1, X_2$  the subset of clocks used by  $G(e_1)$  and  $G(e_2)$  respectively.

$$\Rightarrow X_1 \cap X_2 = \emptyset$$

In this case the two guards  $G(e_1)$  and  $G(e_2)$  cannot be true at the same date, according to the constraint of determinism of the automaton.

### 3.1 Untimed DEVS Syntactic Transformation

We begin by a definition of the syntactic transformation of a TIOA into a DEVS model.

Relationships between sets :

- $S = Q$ , the set of discrete states is the same in the two models.
- $X_M = I$ , the set of input events of the TIOA model represents the set of input event variables in the DEVS model.
- $Y_M = O$ , the set of output events in the TIOA represents the set of output event variables in the DEVS model.

Relationships between functions :

$\forall e_i \in E$  :

- External transition function  $-\delta_{\text{ext}}-$ :

if  $\text{act}(e_i) \in I$  then  $\delta_{\text{ext}}(\text{src}(e_i), e, \text{act}(e_i)) = \text{trg}(e_i)$

- Internal transition function  $-\delta_{\text{int}}-$ :

If  $\text{act}(e_i) \in O$  the  $\delta_{\text{int}}(\text{src}(e_i)) = \text{trg}(e_i)$   
and  $\lambda(\text{src}(e_i)) = \text{act}(e_i)$

**Example:** See the untimed automaton in Figure 2.

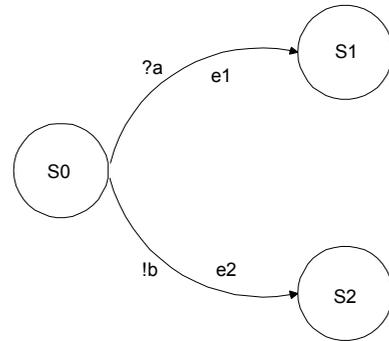


Figure 2: A Simple Untimed Automaton

Defined by :

- $Q = \{s_0, s_1, s_2\}$
- $E = \{e_1, e_2\}$
- $\Sigma = \{I = \{a\}, O = \{b\}\}$
- **src:**  
 $\text{src}(e_1) = \text{src}(e_2) = s_0$
- **act:**  
 $\text{act}(e_1) = a; \text{act}(e_2) = b$
- **trg:**  
 $\text{trg}(e_1) = s_1; \text{trg}(e_2) = s_2$

becomes, in DEVS :

- $S = Q = \{s_0, s_1, s_2\}$
- $XM = \{a\}$
- $YM = \{b\}$
- $e_1 :$

$$\begin{aligned} \text{act}(e_1) = a \in I &\Rightarrow \delta_{\text{ext}}(\text{src}(e_1), e, \text{act}(e_1)) = \text{trg}(e_1) \\ &\Rightarrow \delta_{\text{ext}}((s_0, e), a) = s_1 \end{aligned}$$

- $e_2 :$

$$\begin{aligned} \text{act}(e_2) = b \in O &\Rightarrow \delta_{\text{int}}(\text{src}(e_2)) = \text{trg}(e_2) \\ &\text{and } \lambda(\text{src}(e_2)) = \text{act}(e_2) \\ &\Rightarrow \delta_{\text{int}}(s_0) = s_2 \\ &\text{and } \lambda(s_0) = b \end{aligned}$$

and the state graph (Figure 3) :

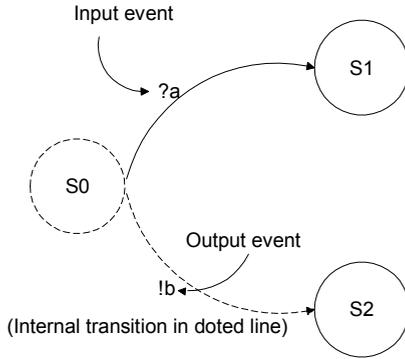


Figure 3: State Graph of the Resulting DEVS Model

This first step gives an untimed DEVS (which can be not deterministic). In order to obtain a complete transformation, we have to introduce new state variables called temporal state variables, a valuation function and to express the lifetime function.

**Definition 13:** A temporal state variable is a variable  $x$  included in a domain  $\text{dom}(x) = J \cup \{\infty\}$ , where  $J$  is an interval over  $\mathbb{R}$ . Let  $C_M$  is the set of state variables.

**Definition 14:** A term over  $C_M$  is an expression generated by the grammar  $z ::= x | n | z + n$ , where  $x \in C_M$  and  $n \in \mathbb{R}$ . Let  $T_M(C)$  be the set of all terms over  $C_M$ .

**Definition 15:** A constraint over  $C_M$  is a Boolean combination  $\phi$  of inequalities of the form  $z \leq z'$  or  $z < z'$  with  $z, z' \in T_M(C_M)$ . The Boolean constants are used to indicate if the constraint is realized or not. Let  $F_M(C_M)$  be the set of all these formulas.

**Definition 16:** A (simultaneous) assignment over  $C_M$  is a function  $\lambda : C_M \rightarrow T_M(C_M)$ . Let  $M_M(C_M)$  be the set of all assignments.

**Definition 17:** A temporal state variable valuation  $v$  is a vector that returns for each state variable  $x \in C_M$  a value

in  $\text{dom}(x)$ . Let  $V_M(C_M)$  be the set of all valuations over  $C_M$ .

**Definition 18:** We define the discrete (or sequential) state of a DEVS model as follow :

$$S_d = \{(s, v) \in S_M \times V_M\}$$

### 3.2 Lifetime Function -D-

According to the first hypothesis, all transition guards of input events are fully determined and can occurred only on one value determined by either an Invariant or a Guard.

$$D : S \times V_M(C_M) \rightarrow \mathbb{R}$$

$\forall s_i \in S :$

- if  $\text{Inv}(s_i) = \emptyset$  then  $D(s_i) = \infty$
- else

the invariant and guard are included in  $F_M(C_M)$ .

Guards and invariants are Boolean combinations of terms of the form  $z \leq z'$  or  $z < z'$  and  $z = z'$ .

Let  $\text{Op} = \{\leq, <, =\}$ :

1. A formula  $z_i \text{ Op } z_i' \wedge z_j \text{ Op } z_j'$  is equivalent to :

$$\min((z_i' - z_i), (z_j' - z_j))$$

2. A formula  $z_i \text{ Op } z_i' \vee z_j \text{ Op } z_j'$  is equivalent to :

$$\max((z_i' - z_i), (z_j' - z_j))$$

3. A combination of this two type of formula is a combination of min-max.
4. Let  $\text{GM}(ei)$  = the result of the combination of this three operations on guard.
5. Let  $\text{InvM}(ei)$  = the result of the combination of this three operations on the invariant.
6. Let  $D(s_i)$  = the result of the min of the combination of this operations on invariant and Guard.

For a given state  $D(s_i)$  depends on the values of the temporal state variables.

### 3.3 Operational Semantics OS(M)-

**Definition 19:** The operational semantics  $\text{OS}(M)$  of a DEVS  $M$  is specified by:

- **Discrete states:**

$$S_d = \{(s, v) \in S_M \times V_M\}$$

- **Total states:**

$$Q_M = \{(S_d, e) = ((s, v), e) \in S_M \times V_M \times R \mid 0 \leq e \leq D(s)\}$$

- **Initial state:**

$$Q_M^0 = ((s^0, v_B^0), 0)$$

$\forall ei \in E$  in the TIOA:

if  $\mathbf{act}(ei) \in \mathbf{I}$  and  $v(C_M) \models G_M(ei)$  then  
 $v = v+e$  and  $v' = v_O A(ei)$  and  
 $\delta_{ext}((src(ei), v(C_M)), act(ei)) = (trg(ei), v')$  and  
 $e := 0$

if  $\mathbf{act}(ei) \in \mathbf{O}$  and  $v(C_M) \models G_M(ei)$  and  $e = D(src(ei))$  then  
 $v = v+e$  and  $v' = v_O A(ei)$  and  
 $\delta_{int}((src(ei), v(C_M))) = (trg(ei), v')$  and  
 $\lambda(trg(ei)) = act(ei)$  and  
 $e := 0$

## 4 EXAMPLE AND SIMULATION

### 4.1 Filling System Example

We consider that the DEVS model of the system to be controlled is in the model base. This system, a filling system, is composed of a tank with a valve, a conveyor and barrels (Figure 4).

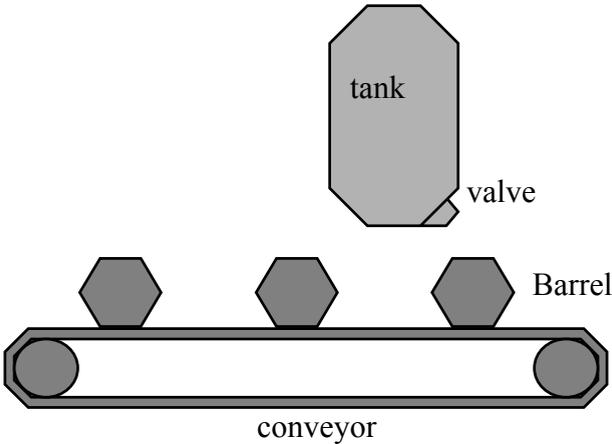


Figure 4: A Simple Filling System

This filling system model has two discrete event inputs:

- Control of the valve : VAL = {Open, Close}
- Control of the conveyor : MOT = {Start, Stop}

And two sensor outputs :

- Barrel level : BL = {Full}
- Barrel position : BP = {Good}

The DEVS model of the filling system is in Figure 5.

One possible specification of the control system by a timed automaton is given in Figure 6.

This Timed Automaton is defined by :

- $Q = \{ \text{Init, Adcon0, Adcon1, Stop, Filling0, Filling1, Error} \}$
- $E = \{e1, e2, e3, e4, e5, e6, e7, e8\}$
- $\Sigma = \{I = \{Bp.Good, Bl.Full\}, O = \{Mot.Start, Mot.Stop, Val.Open, Val.Close\}\}$

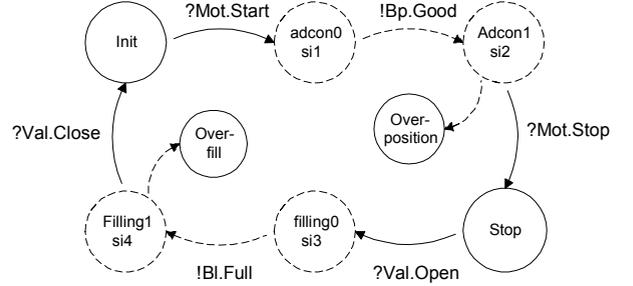


Figure 5: DEVS Model of the Filling System

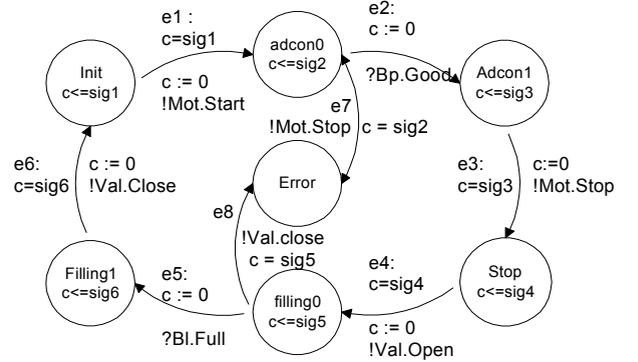


Figure 6: Timed Automaton of the Control System

- src:  
 $src(e1) = \text{Init}; \quad src(e2) = \text{Adcon0};$   
 $src(e3) = \text{Adcon1}; \quad \dots$
- act:  
 $act(e1) = \text{Mot.Start}; \quad act(e2) = \text{Bp.Good};$   
 $act(e3) = \text{Mot.Stop}; \quad \dots$
- trg:  
 $trg(e1) = \text{Adcon0}; \quad trg(e2) = \text{Adcon1};$   
 $trg(e3) = \text{Stop}; \quad \dots$
- $q^0 = \text{Init}$

Timing annotation :

- $C = \{c\}$
- Inv:  
 $Inv(\text{Init}) = (c \leq sig1); \quad Inv(\text{Adcon0}) = (c \leq sig2);$   
 $Inv(\text{Adcon1}) = (c \leq sig3); \quad Inv(\text{Stop}) = (c \leq sig4);$   
 $Inv(\text{Filling0}) = (c \leq sig5); \quad Inv(\text{Filling1}) = (c \leq sig6);$   
 $Inv(\text{Error}) = \emptyset$
- G :  
 $G(e1) = (c = sig1); \quad G(e2) = \emptyset;$   
 $G(e3) = (c = sig3); \quad G(e4) = (c = sig4);$   
 $G(e5) = \emptyset; \quad G(e6) = (c = sig6);$   
 $G(e7) = (c = sig2); \quad G(e8) = (c = sig5)$
- A:  
 $A(e1) = A(e2) = A(e3) = A(e4) = A(e5) = A(e6) = (c := 0)$   
 $A(e7) = A(e8) = \emptyset$
- $v^0 = \{0\}$

Now, in order to verify this specification by simulation, we transform this model into a DEVS atomic model :

Step 1 : untimed DEVS :

- $S=Q=$   
 $\{\text{Init}, \text{Adcon0}, \text{Adcon1}, \text{Stop}, \text{Filling0}, \text{Filling1}, \text{Error}\}$
- $X_M = I = \{\text{Bp.Good}, \text{Bl.Full}\}$
- $Y_M = O = \{\text{Mot}, \text{Val}\}$
- $s^\circ = q^\circ = \text{Init}$
- $C_M = \{c\}$
- $v^\circ(C_M) = \{0\}$
- $\text{Act}(e1) \in O$   
 $\Rightarrow \delta_{\text{int}}(\text{src}(e1)) = \text{trg}(e1)$   
 and  $\lambda(\text{trg}(e1)) = \text{act}(e1)$   
 $\Rightarrow \delta_{\text{int}}(\text{Init}) = \text{Adcon0}$   
 and  $\lambda(\text{Adcon0}) = \text{/Mot.Start}$
- $\text{Act}(e2) \in I$   
 $\Rightarrow \delta_{\text{ext}}((\text{src}(e2), e), \text{act}(e2)) = \text{trg}(e2)$   
 $\Rightarrow \delta_{\text{ext}}((\text{Adcon0}, e), \text{Bp.Good}) = \text{Adcon1}$

...

Step 2 : Transformation in atomic DEVS :

We add state variable sets :

$$C_M = \{c\}$$

and the initial valuation of state variable  $c$  :

$$v^\circ(C_M) = \{0\}$$

Operational semantics :

Total states :

$$Q_M = \{((\text{Init}, v), e), ((\text{Adcon0}, v), e), ((\text{Adcon1}, v), e), ((\text{Stop}, v), e), ((\text{Filling0}, v), e), ((\text{Filling1}, v), e), ((\text{Error}, v), e)\}$$

$$Q^\circ = ((\text{Init}, v), e)$$

Lifetime Function :

$$\begin{aligned} \text{Inv}(\text{Init}) &= (c \leq \text{sig1}) \Rightarrow D(\text{Init}) = \text{sig1} - v(c) \\ \text{Inv}(\text{Adcon0}) &= (c \leq \text{sig2}) \Rightarrow D(\text{Adcon0}) = \text{sig2} - v(c) \\ \text{Inv}(\text{Adcon1}) &= (c \leq \text{sig3}) \Rightarrow D(\text{Adcon1}) = \text{sig3} - v(c) \\ \text{Inv}(\text{Stop}) &= (c \leq \text{sig4}) \Rightarrow D(\text{Stop}) = \text{sig4} - v(c) \\ \text{Inv}(\text{Filling0}) &= (c \leq \text{sig5}) \Rightarrow D(\text{Filling0}) = \text{sig5} - v(c) \\ \text{Inv}(\text{Filling1}) &= (c \leq \text{sig6}) \Rightarrow D(\text{Filling1}) = \text{sig6} - v(c) \\ \text{Inv}(\text{Error}) &= \emptyset \Rightarrow D(\text{Error}) = \infty \end{aligned}$$

Then internal and external transition functions become:

$$\begin{aligned} \text{Act}(e1) \in O &\Rightarrow \text{if } v \models G_M(e1) \text{ and } e = D(\text{src}(e1)) \\ &\Rightarrow \text{if } v \models (c = \text{sig1}) \text{ and } e = D(\text{Init}) \\ &\Rightarrow \text{if } v \models (c = \text{sig1}) \text{ and } e = \text{sig1} - v(c) \\ &\Rightarrow v = v + e \text{ and } v' = v \circ A(e1) \\ &\Rightarrow \delta_{\text{int}}((\text{Init}, v)) = (\text{Adcon0}, v') \\ &\text{and } \lambda((\text{Init}, v')) = \text{/Mot.Start}; \end{aligned}$$

$$\begin{aligned} \text{Act}(e2) \in I &\Rightarrow \text{if } v \models \emptyset \\ &\Rightarrow v = v + e \text{ and } v' = v \circ A(e2) \\ &\Rightarrow \delta_{\text{ext}}(((\text{Adcon0}, v), e), \text{Bp.Good}) = \\ &(\text{Adcon1}, v') \end{aligned}$$

...

In this case  $c$  has the same behavior than  $e$ ,  $c$  is unused. The final DEVS state graph is in Figure 7.

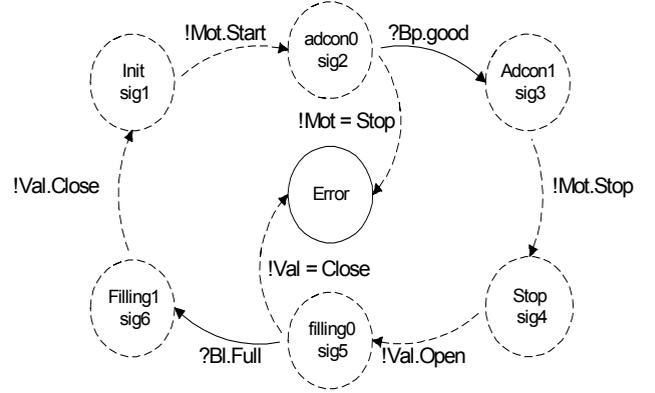


Figure 7: Final State Graph of the DEVS Model of the Control System

## 4.2 Coupled Model and Simulation

The coupled model is built with the control model and the system model by connecting the input/output ports of the two basic models (Figure 8).

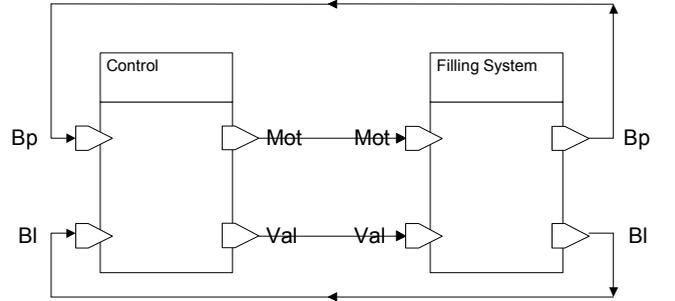


Figure 8: Coupled Model of the Control and the Filling System

Simulation :

Global Clock  $T = 0$ .

$v^\circ(C_M) = \{0\}$ .

Let the DEVS model of the system (Figure 9) :

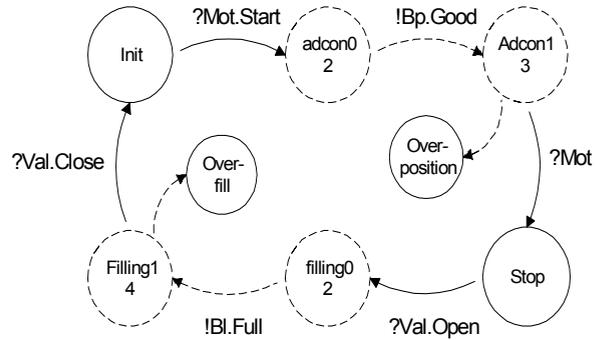


Figure 9: DEVS Model of the Filling System

The following tables give the timed evolution of the coupled model (Table 1).

Table 1: Simulation Table

System DEVS Model								
Event Date (t.u.)	Current state	Timelife D	External transition function(ext)	Internal transition function(int)	Trans. Date	Output function (O)	Output	Next state
0	Init	Infinite	ext((init.e),?Mbt.Start)		1			Adcon0
1	Adcon0	si1=2		int(Adcon0)	3	O(Adcon0)	!Bp.Good	Adcon1
3	Adcon1	si2=3		int(Adcon1)				Over-pos.
"	"	"	ext((Adcon1.e),?Mbt.Stop)		4			Stop
4	Stop	Infinite	ext((Stop.e),?Val.Open)		6			Filling0
6	Filling0	si3=2		int(Filling0)	8	O(Filling0)	!Bl.Full	Filling1
8	Filling1	si4=4		int(Filling1)				Over-fill
"	"	"	ext((Filling1.e),?Val.Close)		11			Init
	Over-Pos.	Infinite						
	Over-Fill	Infinite						

Control DEVS Model								
Event Date (t.u.)	Current state	Timelife D	External transition function(ext)	Internal transition function(int)	Trans. Date	Output function (O)	Output	Next state
0	Init	sig1=1		int(Init.v)	1	O(Init.v)	!Mbt.Start	(Adcon0.v)
1	Adcon0	sig2=3	ext(((Adcon0.v.e),?Bp.Good)		3			(Adcon1.v)
"	"	"		int(Adcon0.v)		O(Adcon0.v)	!Mbt.stop	(Error.v)
3	Adcon1	sig3=1		int(Adcon1.v)	4	O(Adcon1.v)	!Mbt.stop	(Stop.v)
4	Stop	sig4=2		int(Stop.v)	6	O(Stop.v)	!Val.Open	(Filling0.v)
6	Filling0	sig5=1		int(Filling0.v)	8	O(Filling0.v)	!Val.Close	(Filling1.v)
"	"	"	ext(((Filling0.v.e),?Bl.Full)					(Error.v)
8	Filling1	sig6=3		int(Filling1.v)	11	O(Filling1.v)	!Val.Close	(Init.v)
	Error	Infinite						

## 5 CONCLUSION

In this paper, we have presented the formal transformation of a TIOA into a DEVS model in order to verify by simulation, high level specifications given by a TIOA.

The proposed methodology seems to be realistic because it allows the simulation of very complex coupled models, for which a formal proof is quite impossible. In addition, going from high level specifications to the low level design need to define deterministic models, which is done for the transformation of a TIOA into DEVS

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